

Math 80 Test 2 Practice test 1 Fall 2015

Fill in the blanks using the words term, factor, sum, product, difference, quotient, base, exponent, power, index, radicand or root.

- 1) (1 pt each) Given $f(x) = (4x + 2)^2(x - 3)$ $4x$ is both a Product and a term, $(4x + 2)^2$ is both a Power and a factor. $x - 3$ is a difference while $(x - 3)$ is a factor and the entire expression is a Product.

- 2) (3 pt) Solve $5|y - 7| - 4 = 11$ Expression your answer in set notation.

$$\begin{aligned} 5|y - 7| - 4 &= 11 \\ 5|y - 7| &= 15 \\ |y - 7| &= 3 \end{aligned}$$

$$\begin{aligned} y - 7 &= 3 \\ \boxed{y} &= \boxed{10} \\ y - 7 &= -3 \\ \boxed{y} &= \boxed{4} \end{aligned}$$

Check

$$\begin{aligned} 5|3| - 4 &= 11 \\ 15 - 4 &= 11 \end{aligned}$$

$$\begin{aligned} 5|-3| - 4 &= 11 \\ 5(3) - 4 &= 11 \end{aligned}$$

ANSWER.

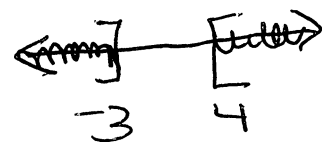
$$\boxed{\{4, 10\}}$$

- 3) (4 pts) Solve $|2k - 1| \geq 7$. Express your solution as both a graph and in interval notation.

$$\begin{aligned} |2k - 1| &\geq 7 \\ 2k - 1 &\leq -7 \text{ OR } 2k - 1 \geq 7 \\ 2k &\leq -6 \text{ OR } 2k \geq 8 \\ \boxed{k} &\leq \boxed{-3} \text{ OR } \boxed{k} \geq \boxed{4} \end{aligned}$$

Check

$$\begin{aligned} k &= -5 & k &= 100 \\ | -11 | &\geq 7 & | 199 | &\geq 7 \\ \text{true} & & \text{true} & \\ k &= 0 & & \\ | -1 | &\geq 7 & & \\ \text{false} & & & \end{aligned}$$



$$(-\infty, -3] \cup [4, \infty)$$

- 4) (3 pts) Solve $-4 < -2|t + 14|$. Express your solution in interval notation.

$$\begin{aligned} \frac{-4}{-2} &> \frac{-2|t + 14|}{-2} \\ 2 &> |t + 14| \\ |t + 14| &< 2 \end{aligned}$$

$$-2 < t + 14 < 2$$

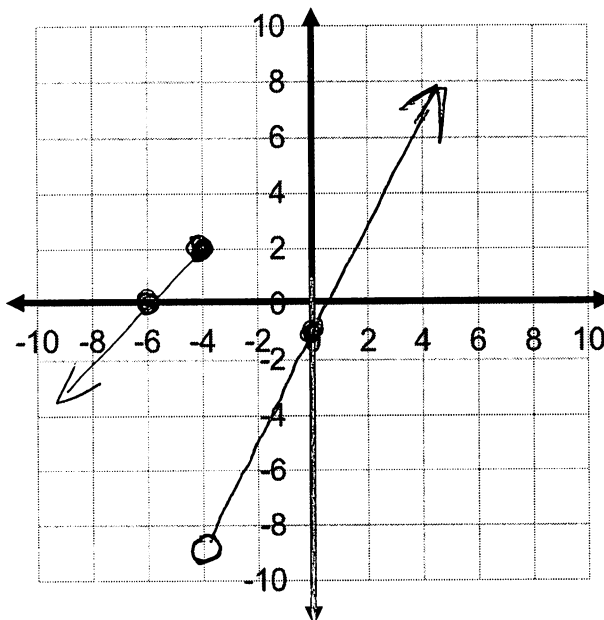
$$\begin{aligned} -2 &< t + 14 < 2 \\ -16 &< t < -12 \end{aligned}$$

$$\begin{aligned} -16 &< t < -12 \\ (-16, -12) \end{aligned}$$

5) Given $f(x) = \begin{cases} x+6 & \text{if } x \leq -4 \\ 2x-1 & \text{if } x > -4 \end{cases}$

a. (1 pt) What's the domain of f ? $(-\infty, \infty)$

b. (4 pts) Graph the function



g. (1 pt) Find $f(-1)$ $2(-1) - 1 = -3$ $f(-1) = -3$

h. (2 pts) Find $f(-4) - f(4)$ $f(-4) - f(4) = 2 - 7 = -5$
 $f(-4) = 2$
 $f(4) = 7$

6) What's the difference between a consistent dependent system and an inconsistent system?

a consistent dependent system has an infinite solution set while an inconsistent system has no solution

- 7) Solve the system using substitution $-9x - 4y = 35$ (4 points)
 $5x + y = -17$

$$5x + y = -17$$

$$y = -17 - 5x$$

$$-9x - 4y = 35$$

$$-9x - 4(-17 - 5x) = 35$$

$$-9x + 68 + 20x = 35$$

$$11x + 68 = 35$$

$$11x = -33$$

$$x = -3$$

- 8) Solve the system using addition $-9x - 4y = -6$ (4 points)
 $5x - 6y = 28$

$$-3(-9x - 4y) = (-6)(-3)$$

$$2(5x - 6y) = (28)(2)$$

$$27x + 12y = 18$$

$$10x - 12y = 56$$

$$\begin{array}{r} 27x + 12y = 18 \\ 10x - 12y = 56 \\ \hline 37x = 74 \end{array}$$

$$x = 2$$

$$5x + y = -17$$

$$5(-3) + y = -17$$

$$y = -2$$

Check

$$-9(-3) - 4(-2)$$

$$27 + 8$$

$$35 \checkmark$$

$$\{(-3, -2)\}$$

$$5x - 6y = 28$$

$$5(2) - 6y = 28$$

$$y = 3$$

Check

$$-9(2) - 4(-3)$$

$$-18 + 12$$

$$-6 \checkmark$$

$$\{(2, -3)\}$$

- 9) After solving the system $\begin{cases} x - 4y = -1 \\ -3x + 12y = 6 \end{cases}$ a student was left with $0 = 3$. Given this result, if you

wrote both equations into the form $y = mx + b$ what would you expect in terms of the slope and the y-intercept?

The value of m would be the same but the y-intercepts would be different. (It's an inconsistent system.)

- 10) Grandma has decided it's a good time to move part of her stock investment into bonds to reduce her risk. She's asked your help in redistributing her \$850,000 between bonds which will earn 4.5% next year and stocks, which she predicts will earn 2% next year. If she needs her investments to bring in \$24,000 in interest (pretax) for the year, how should her investments be redistributed? (Round your answers to the nearest dollar and **you must use a system of equations to answer the question.**)

Grandma should put \$ 280,000 into bonds.
 " " " \$ 570,000 " stocks

$$\begin{aligned} \text{total investment} &= \text{Bond investment} + \text{stock invest.} \\ \underline{850,000} &= \quad \quad \quad X \quad \quad \quad + \quad \quad \quad y \end{aligned}$$

$$\begin{aligned} \text{total interest} &= \text{Bond interest} + \text{stock interest} \\ \underline{24,000} &= \quad \quad \quad 0.045X \quad \quad \quad + \quad \quad \quad 0.02y \end{aligned}$$

$$\begin{aligned} X + y &= 850,000 \\ \text{so} \\ y &= 850,000 - X \end{aligned}$$

$$0.045X + 0.02y = 24,000$$

$$0.045X + 0.02(850,000 - X) = 24,000$$

$$0.045X + 17,000 - 0.02X = 24,000$$

$$\underline{0.025X = 7,000} \quad \text{so} \quad X = 280,000$$

$$\begin{aligned} \frac{0.025}{0.025} \quad \frac{7,000}{0.025} \quad y &= 850,000 - X \\ &= 570,000 \end{aligned}$$